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PARTICLE FILTER WITH HYBRID IMPORTANCE FUNCTION FOR JOINT SYMBOL **DETECTION AND PHASE TRACKING**

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ABSTRACT

In digital communication, phase distortions introduced by local oscillators is one of the major concerns in designing low-cost high frequency wireless communication systems. Hence, for phase tracking and symbol detection, we propose an original algorithm which performs both phase tracking and symbol detection by a particle filtering based on the hybrid importance function. Performances of this algorithm are analyzed and compared to phaselocked loop performances in terms of bit error rate and mean square error. Asymptotic posterior Cramér-Rao bound is also derived to show performances of the optimum receiver.

Keywords : Phase tracking, Particle filter, Hybrid importance function, Decision feedback loop, Asymptotic posterior Cramér-Rao bound.

1. INTRODUCTION

Synchronization is an important practical problem in communication systems. Indeed, non perfect local oscillators used in the receiver and the transmitter seriously damage the baseband received signal. These distortions correspond to the constant shift between the frequency clocks of the transmitter and the receiver and to the random jitter in frequency, known as phase noise, coming from electronic components. Moreover, the phase noise effect is much more significant when the carrier frequency of the digital communication system is large [1, 2] so that it has to be seriously fought against when designing future 40 GHz or 60 GHz communication systems.

The induced time variation of the frequency carrier is estimated and eliminated by a phase tracking device among which the phase-locked loop (PLL) and its digital version (DPLL) are the most commonly used devices.

Recent developments in signal processing and digital communications have shown that it is possible to avoid such approximations by using particle filters. Many wireless communication problems have been solved with success in that way [3] including detection in fast fading channels [4] and multiuser detection in fading code division multiple access (CDMA) channels [5].

In [6], phase noise tracking performance with a prior importance function based particle filter has been examined in a bandlimited additive gaussian channel distortions and compared to phase-locked loop in term of Asymptotic Mean Square Error. In this approach, only the phase tracking problem has been considered.

In this paper, we focus our attention on the joint estimation of phase distortions and transmitted symbols. We propose a particle filter based on the hybrid importance function (PF-SDPT) introduced by Huang and Djuric [7]. Let us note that in [8], authors have proposed an algorithm which combines particle filtering and extended kalman filtering for this joint estimation. However, this approach does not take into account the linear drift and requires the linearization of the dynamic state space model which limits its performance especially when the phase noise rate increases.

The paper is organised as follows :

In section 2, the digital bandlimited communication system and the phase distortion model are described. Section 3 is devoted to particle filtering. We describe the proposed particle filter algorithm for joint phase tracking and symbol detection. Results are given in section 4. The proposed algorithm is compared to the decision feedback loop (DFL) and particle filter algorithm (PF-PT) proposed by [6] in terms of bit error rate (BER) and mean square error (MSE) of phase estimation. We also derive the asymptotic posterior Cramér-Rao bound (PCRB) which corresponds to the lowest achievable MSE in the estimation of phase distortions.

2. SYSTEM MODEL

We consider the baseband communication system in a bandlimited gaussian channel shown in Fig. 1. Phase distortions at the receiver result from two phenomena. One is the constant shift between the frequency clocks of the transmitter and the receiver. The other is the random jitter introduced by the thermal noise of electronic components, known as phase noise. The constant drift and the phase noise are modeled by a multiplicative term p(t) after the pulse shape filtering. In the case of an AWGN channel, p(t)takes into account the phase noise produced by both the transmitter and the receiver.

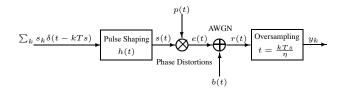


Fig. 1. Baseband system model.

In a baseband complex equivalent form, the carrier delivered by the noisy oscillator can be modeled as :

$$p(t) = \exp(j\theta(t)) \tag{1}$$

where the phase distortion $\theta(t)$ is a Brownian process with a linear drift [1]. Its power spectral density has a Lorentzian shape controlled by the parameter β representing the two-sided 3dB bandwidth. This model produces a $1/f^2$ type noise power behavior that agrees with experimental measurements carried out on real RF oscillators. The phase noise rate is characterized by the bandwidth β normalized with respect to the symbol rate 1/Ts, namely by the parameter βTs .

At the sampling rate of the receiver η/Ts , the discrete form of the phase distortion is :

$$\theta_k = \theta_{k-1} + \varepsilon + v_k \tag{2}$$

where ε is the unknown constant drift between the transmitter and the receiver and v_k is a zero mean gaussian variable with variance $\sigma_v^2 = 2\pi\beta T s/\eta.$

The baseband transmitter delivers i.i.d symbols, which belong to an alphabet A, going through a pulse shaping filter. At the receiver, the maximum likelihood detection can be carried out either on the sampled signal following the matched filter, or directly from the oversampled received signal. In the first case, the Nyquist criterion for bandlimited transmission is not fulfilled, since phase noise causes additive and multiplicative distortions that are statistically intractable [9]. As a consequence, particle filter implementation after the matched filter is inappropriate.

Thereby, we focus on the maximum likelihood detection performed on the received signal which is oversampled by a factor η . In order to avoid Intersymbol Interference (ISI) at each sampling point, a *multi-Nyquist pulse* is used at the transmitter [10, 11].

2.1. Dynamic state space model

At the receiver side, the two unknown states are the transmitted symbols and the phase distortions. The nonlinear state space model can then be written as follows :

$$\begin{cases} \theta_k = \theta_{k-1} + \varepsilon + v_k, & \varepsilon : \text{ unknown constant} \\ y_k = \exp(j\theta_k)s_{\lfloor \frac{k}{\eta} \rfloor} + B_k \end{cases}$$
(3)

where $B_k \sim NC(0, \sigma_B^2)$ is a circular zero mean gaussian white noise with power σ_B^2 and $v_k \sim N(0, \sigma_v^2)$ is a zero mean gaussian white noise with variance σ_v^2 . The operator |X| represents the largest integer lower than or equal to X. The system state is a three dimensional vector $\left(\varepsilon, s_{\lfloor \frac{k}{\eta} \rfloor}, \theta_k\right)$ where the phase varies at each sampling time, the symbols vary at each symbol time and ε is constant during all the transmission and independent of both v_k and the transmitted symbols. Moreover, the oversampling is at the origin of the following relation :

$$\forall k \in \{1 + i\eta, ..., (1 + i)\eta - 1 | i \in \mathbb{Z}\}, s_{\lfloor \frac{k}{2} \rfloor} = s_{\lfloor \frac{k-1}{2} \rfloor} \quad (4)$$

3. PARTICLE FILTER

3.1. Introduction

The maximum a posteriori (MAP) estimation of the state from the measurement is obtained in the framework of the Bayesian theory which has been mainly investigated in Kalman filtering [12]. The Kalman filter is optimal when state and measurement equations are linear and noises are independent, additive and gaussian. When these assumptions are not fulfilled, various approximation methods have been developed among which the extended Kalman filter (EKF) is the most commonly used technique [12].

Since the nineties, particle filters have become a powerful methodology to cope with non-linear and non gaussian problems [13] and an important alternative to the EKF. The advantage lies in an approximation of the distribution of interest by discrete random measures, which does not involve any linearization.

Based on sequential importance sampling, particle filtering is an extension of the sequential Monte Carlo methodology [14]. It consists in recursively computing the required posterior density function $p(x_{0:k}|y_{0:k})$ by approximating by a set of N random samples with associated weights, denoted by $\{x_{0:k}^{(m)}, w_k^{(m)}\}_{m=1..N}$:

$$\widehat{p}(x_{0:k}|y_{0:k}) = \sum_{j=1}^{N} \delta(x_{0:k} - x_{0:k}^{(j)}) \widetilde{w}_{k}^{(j)}$$
(5)

u

where $x_k^{(j)}$ is drawn from the importance function $\pi(x_k | x_{0:k-1}^{(m)}, y_{0:k}), \delta(.)$ is the Dirac delta function and $\widetilde{w}_k^{(j)} = w_k^{(j)} / \sum_{m=1}^N w_k^{(m)}$ is the normalized importance weight associated with the *j*-th particle. The weights $w_k^{(m)}$ are updated according the concept of importance of importance of moments as a sampling.

portance sampling :

$$y_k^{(m)} \propto \frac{p(y_k | x_{0:k}^{(m)}) p(x_k^{(m)} | x_{0:k-1}^{(m)})}{\pi(x_k^{(m)} | x_{0:k-1}^{(m)}, y_{0:k})} w_{k-1}^{(m)}$$
(6)

In order to overcome the degeneracy problems of particle filtering after few iterations [14, 15], we integrate in the algorithm a resampling step as in [16].

Performances of particle filter mainly depend on the choice of the importance function. The most common choices are the prior density function and the optimal density function. The first one is the most widely used [17], which is largely due to the implementation simplicity. However, this distribution does not incorporate any information contained in the most recent observation and, therefore, may be inefficient and especially sensitive to outliers. The optimal density based particle filter has been introduced in [18]. In this paper, Zaritskii has shown that it minimizes the variance of the importance weights $\widetilde{w}_k^{(m)}$ conditional upon the particle trajectories $x_{0:k}^{(m)}$ and the observations $y_{0:k}$. When dealing with a state process which can be divided into two independent parts, Huang and Djuric have proposed the hybrid importance function [7] which combines the prior and the optimal density.

3.2. Particle filtering for phase tracking and symbol detection

In this paragraph, we develop particle filter based on the hybrid (PF-SDPT) for joint phase distortion estimation and symbol detection.

The design of the particle filter requires both a simulation method for the generation of particles and the formula for updating importance weights. Since the state vector we want to estimate $x_k = \left(\varepsilon, \theta_k, s_{\lfloor \frac{k}{\eta} \rfloor}\right)$ includes three processes among which only the phase θ_k and the transmitted symbol $s_{\lfloor \frac{k}{\eta} \rfloor}$ are time varying, the particle generation is carried out at steps 0 and 1. The step 0 consists in drawing each particle coordinate $\{\varepsilon^{(m)}\}_{m=1..N}$ according to the uniform law on a predefined range and does not depend on the importance function unlike steps 1 and 2.

In our context, this hybrid importance function can be written as :

$$\pi(s_{\lfloor \frac{k}{\eta} \rfloor}, \theta_k | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}^{(m)}, \theta_{0:k-1}^{(m)}, y_{0:k}) = p(\theta_k | \theta_{k-1}^{(m)}) \times p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}^{(m)}, \theta_{0:k}^{(m)}, y_{0:k})$$
(7)

where and,

$$p(\theta_k | \theta_{k-1}^{(m)}) = N(\theta_k; \theta_{k-1}^{(m)} + \varepsilon^{(m)}, \sigma_v^2)$$
(8)

$$p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}^{(m)}, \theta_{0:k}^{(m)}, y_{0:k}) = \frac{p(y_k | s_{\lfloor \frac{k}{\eta} \rfloor}, \theta_k^{(m)}) p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k}{\eta} \rfloor}^{(m)})}{\sum_{s_{\lfloor \frac{k}{\eta} \rfloor} \in A} p(y_k | \theta_k^{(m)}, s_{\lfloor \frac{k}{\eta} \rfloor})}$$

$$(9)$$

This last expression can be simplified when k is a multiple of η by :

$$p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}, \theta_{0:k}, y_{0:k}) = \frac{p(y_k | s_{\lfloor \frac{k}{\eta} \rfloor}, \theta_k)}{card(A)p(y_k | \theta_k, s_{\lfloor \frac{k-1}{\eta} \rfloor})}$$
(10)

where

$$p(y_k|\theta_k, s_{\lfloor \frac{k}{\eta} \rfloor}) = NC(y_k; s_{\lfloor \frac{k}{\eta} \rfloor} e^{j\theta_k}, \sigma_B^2)$$
(11)

Otherwise, (9) takes the form :

$$p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}, \theta_{0:k}, y_{0:k}) = \begin{cases} 1 & \text{if } s_{\lfloor \frac{k}{\eta} \rfloor} = s_{\lfloor \frac{k-1}{\eta} \rfloor} \\ 0 & \text{otherwise} \end{cases}$$
(12)

The PF-SDPT does not take into account the received signal for sampling θ_k . Indeed, we draw N samples $\theta_k^{(m)}$ from the prior probability density function $p(\theta_k | \theta_{0:k-1}^{(m)})$ given by (8). In this context, the update of the weights can be computed using (11) as :

$$w_k^{(m)} \propto \frac{1}{card(A)} \sum_{s_{\lfloor \frac{k}{\eta} \rfloor} \in A} p(y_k | s_{\lfloor \frac{k}{\eta} \rfloor}, \theta_k^{(m)}) w_{k-1}^{(m)}$$
(13)

, if k is a multiple of η .

$$w_k^{(m)} \propto p(y_k | s_{\lfloor \frac{k}{\eta} \rfloor} = s_{\lfloor \frac{k-1}{\eta} \rfloor}, \theta_k^{(m)}) w_{k-1}^{(m)}$$
(14)

, otherwise.

Every element required in the implementation of the particle filtering algorithm have been identified. The miniminum mean square error (MMSE) estimate of θ_k can be easily calculated according to :

$$\widehat{\theta}_k^{mmse} = \sum_{j=1}^M \theta_k^{(j)} \widetilde{w}_k^{(j)}$$
(15)

and the maximum a posteriori (MAP) estimate of the data performed at the end of each symbol (i.e. k + 1 multiple of η) is

$$\widehat{s}_{\lfloor \frac{k}{\eta} \rfloor}^{map} = argmax_{s_{\lfloor \frac{k}{\eta} \rfloor}} \left\{ \sum_{j=1}^{M} \widetilde{w}_{k}^{(j)} \delta((\theta_{k}, s_{\lfloor \frac{k}{\eta} \rfloor}) - (\theta_{k}, s_{\lfloor \frac{k}{\eta} \rfloor})^{(j)}) \right\}$$
(16)

The PF-SDPT algorithm is summed up in Table 1.

For each particle $m \in \{1, ..., N\}$:

0. Draw $\varepsilon^{(m)}$ from the uniform distribution on the range $[0;\Delta/\eta]$

At the k-th iteration, for each particle $m \in \{1, ..., N\}$: 1. (a) Draw particles using (8) :

$$\theta_k^{(m)} \sim p(\theta_k | \theta_{k-1}^{(m)})$$

(b) Draw particles :

$$s_{\lfloor \frac{k}{\eta} \rfloor}^{(m)} \sim p(s_{\lfloor \frac{k}{\eta} \rfloor} | s_{0:\lfloor \frac{k-1}{\eta} \rfloor}^{(m)}, \theta_{0:k}^{(m)}, y_{0:k})$$

If k multiple of $\eta,$ use (10) and (11) else, use (12)

2. Evaluate the importance weights :

$$w_k^{(m)} \propto p(y_k | \theta_k^{(m)}, s_{\lfloor rac{k-1}{\eta}
floor}^{(m)}) w_{k-1}^{(m)}$$

If k multiple of η , use (13) else, use (14).

- 3. Normalize the importance weights : $\tilde{w}_k^{(j)} = 1/\sum_{m=1}^N w_k^{(m)}$
- 4. Resampling step if $N_{eff} < N/2$

4. RESULTS

The performance of the proposed particle filtering algorithm using hybrid importance function is studied for a binary phase shift keying (BPSK) modulation. We have randomly generated 2,000 signal bursts of duration $T = 500 \ Ts$ (i.e., 1,000,000 bits). The linear drift ε is set at $0.5/\eta$ which corresponds to a very bad synchronization. The particle filter algorithms have been implemented with 600 particles.

Let us note that the DFL and the PF-PT described in [6] are only phase tracking algorithms. Indeed, the maximum likelihood detection is carried out on the η available samples of the received signal after phase distortion correction. In the proposed PF-SDPT, phase distortions and symbols are jointly estimated according to respectively MMSE and maximum *a posteriori* criteria.

Figure 2 shows the performance in term of BER achieved for different phase noise rates and with an oversampling factor $\eta = 4$. It can be seen that the proposed PF-SDPT algorithm outperforms the DFL and the PF-PT whatever the signal-to-noise ratio (SNR). However smaller the SNR is, closer are the curves. The Mean Square Error (MSE) of the phase distortion estimates depicted in Figure 3 is obtained by :

$$MSE = E\left[\left((\theta_k - \widehat{\theta}_k)[2\pi]\right)^2\right]$$

where $\hat{\theta}_k$ is the phase distortion estimate at time k. This MSE confirms that estimation is achieved by PF algorithms with a better accuracy. We can denote that MSE is always weaker with the PF-SDPT than with other algorithms. We can also remark in Figure 3 that the PF-SDPT is more robust when the phase noise rate increases. At 20 dB, MSE of PF-SDPT and PF-PT are close to the optimum (asymptotic PCRB analytically derived in Appendix A) up to respectively $\beta Ts = 0.05$ and $\beta Ts = 0.04$. When the phase noise rate increases, the MSE increases rapidly due to the

symbol error detection. Even if the MSE performances of the two PF algorithms are very close at high SNR and for a low phase noise rate, symbol detection by PF-SDPT is nevertheless better achieved than by PF-PT (Fig. 2). Since the PF-PT corrects the phase before the symbol detection, its performance in term of BER is related directly to the quality of the phase distortion estimate. On the other hand for the PF-SDPT, the symbol detection is based on the MAP criterion and performed jointly with the phase tracking, which improves to him more robustness and thus a greater effectiveness in detection.

Finally, we study the influence of the oversampling factor. Figure 4 represents the BER versus phase noise rate for two different values of η and with a SNR fixed at 10 dB. The figure shows that with $\eta = 2$, the BER curves for all the algorithms degrade faster but they are still efficient for a low phaseSfoigereplacements The results of the proposed approaches are still better than the PF-PT and the DFL results.

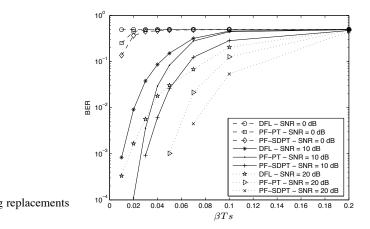


Fig. 2. BER of the algorithms versus phase noise rate βTs with three different SNR and $\eta = 4$.

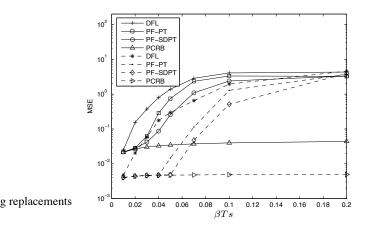


Fig. 3. MSE of the algorithms versus phase noise rate βTs with SNR = 10 dB (solid lines) and SNR = 20 (dashed lines).

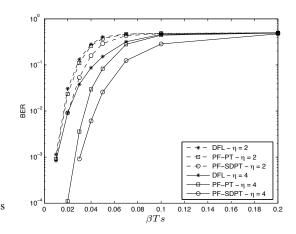


Fig. 4. BER of the algorithms versus phase noise rate βTs with two different oversampling factors with SNR = 10 dB.

5. CONCLUSION

In this paper, we have considered the problem of phase synchronization in digital communications. To solve this problem, we have proposed a particle filter based on the hybrid importance function. The main originality of this work is the joint estimation of phase distortions and transmitted symbols by particle filtering based on the hybrid importance function. This one takes advantages of both the posterior and the prior importance function. Moreover, the algorithms are implemented in the case of multiple samples per symbol, which provides implicit diversity and allows a better phase tracking. Numerical simulations demonstrate the effectiveness of the proposed PF-SDPT algorithm compared to the PF-PT and the DFL both in terms of BER and MSE of the phase estimate.

Appendix A - Posterior Cramér-Rao bound.

Here, we wish to derive the PCRB associated to the phase distortion process $(\theta_k, \varepsilon_k)$ in order to obtain a lower bound for the MSE of the phase distortion estimates. Under the model (3), the Fisher information matrix (FIM) for $(\theta_k, \varepsilon_k)$ can be denoted by :

$$J_k = \begin{pmatrix} J_k^{11} & J_k^{12} \\ J_k^{21} & J_k^{22} \end{pmatrix}$$

that can be obtained by a recursive method which sequentially evaluates the inverse MSE of $(\theta_k, \varepsilon_k)$ as shown in [19]:

$$J_{k+1}^{11} = H_k^{33} - \frac{(H_k^{13})^2}{J_{k-1}^{11} + H_k^{11}}$$
(17)

$$J_{k+1}^{12} = J_{k+1}^{21} = H_k^{23} - \frac{H_k^{13}(J_k^{12} + H_k^{12})}{J_k^{11} + H_k^{11}}$$
(18)

$$J_{k+1}^{22} = J_k^{22} + H_k^{22} - \frac{(J_k^{12} + H_k^{12})^2}{J_k^{11} + H_k^{11}}$$
(19)

Elements of matrix H_k are obtained as follows :

$$H_k^{11} = E[-\Delta_{\theta_k}^{\theta_k} \log p_k]$$
(20)

$$H_k^{12} = E[-\Delta_{\theta_k}^{\varepsilon_k} \log p_k]$$
(21)

$$H_k^{13} = E[-\Delta_{\theta_k}^{\theta_{k+1}} \log p_k]$$
(22)

$$H_k^{22} = E[-\Delta_{\varepsilon_k}^{\varepsilon_k} \log p_k]$$
(23)

$$H_k^{23} = E[-\Delta_{\varepsilon_k}^{\circ k+1} \log p_k]$$
(24)

$$H_k^{33} = E[-\Delta_{\theta_{k+1}}^{\theta_{k+1}} \log p_k]$$
(25)

where

$$p_{k} = p(\theta_{k+1}|\theta_{k},\varepsilon_{k})p(y_{k+1}|\theta_{k+1},s_{\lfloor\frac{k+1}{n}\rfloor})$$
(26)

and, Δ denotes the second derivative operator, defined as $\Delta_{\varepsilon_k}^{\theta_{k+1}} = \partial^2 / \partial \varepsilon_k \partial \theta_{k+1}$ and log(.) is the natural logarithm. Using equations (8) and (11), we obtain :

$$H_k^{11} = 1/\sigma_v^2$$
 (27)

$$H_k^{12} = 1/\sigma_v^2$$
(28)

 $H_k^{13} = -1/\sigma_v^2 \tag{29}$

$$H_k^{22} = 1/\sigma_v^2 \tag{30}$$

$$H_k^{23} = -1/\sigma_v^2$$
(31)

$$H_k^{33} = \frac{1}{\sigma_v^2} + \frac{E[2|s_{k+1}|^2]}{\sigma_B^2} = \frac{1}{\sigma_v^2} + \frac{2}{\sigma_B^2}$$
(32)

Then, assuming that J_{k+1}^{11} converges and using (17), (20), (22) and (25), we obtain for its limit the following result :

$$J_{\infty}^{11} = \frac{2\sigma_v^2 \pm 2\sqrt{\sigma_v^2(\sigma_v^2 + 2\sigma_B^2)}}{2\sigma_v^2 \sigma_B^2}$$
(33)

In the same way, $J_{\infty}^{12} = -1/\sigma_v^2$ and J_{∞}^{22} diverges. Consequently, it is sufficient to assume that the parameter ε_k is known. With this assumption, the Fisher information matrix J_k corresponds to the J_k^{11} and follows the recursion :

$$J_{k+1} = \frac{1}{\sigma_v^2} + \frac{2}{\sigma_B^2} - \frac{1/\sigma_v^4}{J_k + 1/\sigma_v^2}$$
(34)

So the Cramér-Rao bound can be written recursively :

$$C_{k+1} = \frac{1}{1/\sigma_v^2 + 2/\sigma_B^2 - \frac{1/\sigma_v^4}{1/C_k + 1/\sigma_v^2}}$$
(35)

Assuming convergence of the sequence, we deduce from (35) its asymptotic bound :

$$C_{\infty} = -\frac{\sigma_v^2}{2} + \frac{\sqrt{\sigma_v^2(\sigma_v^2 + 2\sigma_B^2)}}{2}$$
(36)

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